

(三十分/20分) Calculus Test

2001/12/21

1. Find the derivatives of the following functions respectively.

- (30%) (a) $f(x) = e^{5x}$ (b) $g(x) = (x^2+5)e^{x^3}$
(c) $h(x) = \ln(x^2+5)$ (d) $r(x) = \ln x^{x^2}$
(e) $s(x) = \ln\left(\frac{x^4}{x^2+5}\right)^2$ (f) $F(x) = e^{\frac{x^4+3x}{x^2+9}}$

2. Find the equation of the tangent line of the following

- (20%) (i) $f'(x) = 5f(x)$, $A(1, f(1))$, $f'(1) = 2$
(ii) $f(x) = 10^x$, $A(0, 1)$

3. Draw the following graph

- (20%) (i) $f(x) = \ln\left(\frac{x^4}{x-1}\right)$, $x > 1$
(ii) $g(x) = e^{-\frac{x^2}{2}}$, $x \in \mathbb{R}$

4. 試求下列積分值

- (35%) (a) $\int_0^1 (x^3+3x+5) dx$ (b) $\int_0^1 \frac{x}{(x^2+3)^2} dx$ (c) $\int_0^2 5x e^{x^2} dx$
(d) $\int_1^2 \frac{5}{x} dx$ (e) $\int_0^1 x e^x dx$

5. 在果蠅數目的實驗培養中：第1天發覺有 100 隻
第3天 " " 300 隻
(5%) 試問：若數目是以指數在增加的模式
則在第5天大約有幾隻果蠅？